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Argon Pressure Drops to and from Condenser

The Argon vapor line to the condenser and liquid line from the condenser are sized for low pressure drop.

Argon Data

Argon physical properties from NIST REPROP

argon liquid density

$$\rho_{Ar_l} := 1396 \cdot \frac{kg}{m^3}$$

argon vapor density

$$\rho_{Ar_v} := 0.4 \cdot \frac{lb}{ft^3}$$

argon liquid visc

$$\mu_{Ar_l} := .261 \cdot cP$$

argon liquid viscosity

$$\mu_{Ar.l} := 0.26 \cdot cpoise$$

argon gas viscosity

$$\mu_{Ar.v} := 0.00717 \cdot cpoise$$

argon heat capacity ratio

$$\gamma_{Ar} := 1.72$$

argon MW

$$MW_{Ar} := 39.948 \cdot \frac{gm}{mole}$$

argon mass flowrate

$$mflow_{Ar} := 208 \cdot \frac{lb}{hr}$$

define parameters for pressure drop calc - Argon vapor to condenser

**Tube Outlet Pressure
assuming 0 psi in condenser**

$$P_{out} := 0 \cdot \text{psi} + \text{atm}$$

Outlet Temperature

$$T_{out} := 88 \cdot \text{K}$$

heat capacity ratio

$$\gamma := \gamma_{Ar}$$

molecular weight

$$M_w := MW_{Ar}$$

viscosity

$$\mu := \mu_{Ar,v}$$

mass flow

$$mflow := mflow_{Ar}$$

Vapor Pipe inside diameter

$$D_v := 2.157 \cdot \text{in}$$

Vapor Pipe Length

$$L_v := 75 \cdot \text{ft}$$

Pipe Roughness:

$$\epsilon := 0.00015 \cdot \text{ft}$$

define initial guesses for calc

Pressure Drop initial guess

$$\Delta P := 0.5 \cdot \text{psi}$$

Pipe Inlet Pressure

$$P_{in} := P_{out} + \Delta P \quad P_{in} - \text{atm} = 0.5 \cdot \text{psi}$$

Temperature Change initial guess

$$\Delta T := 0.05 \cdot \text{K}$$

Inlet Temperature

$$T_{in} := T_{out} + \Delta T$$

Friction factor initial guess

$$f := 0.004$$

Calc vapor pipe velocity

$$V_1 := \frac{\frac{mflow}{\rho_{Ar_v}}}{\left(\frac{D_v}{2}\right)^2 \cdot \pi} = 5.692 \cdot \frac{\text{ft}}{\text{s}}$$

Calc Reynolds number

$$Re_{num} := \frac{V_1 \cdot D_v \cdot \rho_{Ar_v}}{\mu} = 84944$$

Pipe Pressure Drop Equations

Given

Fanning Friction Factor traditional straight pipe

$$\frac{1}{\sqrt{f}} = -4.0 \cdot \log \left(\frac{\epsilon}{3.7 \cdot D_v} + \frac{1.255}{4 \cdot \frac{mflow}{D_v \cdot \pi \cdot \mu} \cdot \sqrt{f}} \right)$$

Adiabatic compressible flow equations

$$\frac{mflow}{\left(\frac{D_v}{2}\right)^2 \cdot \pi} = \sqrt{2 \cdot \frac{M_w}{R_g} \cdot \left(\frac{\gamma}{\gamma - 1}\right) \cdot \left[\frac{T_{out} - T_{in}}{\left(\frac{T_{in}}{P_{in}}\right)^2 - \left(\frac{T_{out}}{P_{out}}\right)^2} \right]}$$

$$\left[\frac{\gamma + 1}{\gamma} \cdot \ln \left(\frac{P_{in} \cdot T_{out}}{P_{out} \cdot T_{in}} \right) - \left(\frac{\gamma - 1}{2 \cdot \gamma} \right) \cdot \left(\frac{P_{in}^2 \cdot T_{out}^2 - P_{out}^2 \cdot T_{in}^2}{T_{out} - T_{in}} \right) \cdot \left(\frac{1}{P_{in}^2 \cdot T_{out}} - \frac{1}{P_{out}^2 \cdot T_{in}} \right) \right] + \frac{4 \cdot f \cdot L_v}{D_v} = 0$$

ref: Chemical Process Safety: Fundamentals with Applications. 2nd ed.

$$\begin{pmatrix} f \\ T_{in} \\ P_{in} \end{pmatrix} := \text{Find}(f, T_{in}, P_{in})$$

Results

| Inlet Pressure | Inlet Temperature | Fanning Friction factor |
|---------------------------------|-----------------------|-------------------------|
| $P_{in} - atm = 0.01 \cdot psi$ | $T_{in} = 88 \cdot K$ | $f = 0.005$ |

Argon Vapor line to HX Pressure Drop

$$P_{in} - P_{out} = 0.015 \cdot psi$$

define parameters for pressure drop calc - Argon liquid from condenser

Tube Inlet Pressure
assuming 0 psi in condenser

$$P_{out} := 0 \cdot \text{psi} + \text{atm}$$

viscosity

$$\mu := \mu_{Ar,I}$$

Liquid Pipe inside diameter

$$D_I := 0.674 \cdot \text{in}$$

Liquid Pipe Length

$$L_I := 125 \cdot \text{ft}$$

Pipe Roughness:

$$\varepsilon := 0.00015 \cdot \text{ft}$$

Liquid Pipe velocity

$$V_I := \frac{\frac{m\text{flow}_{Ar}}{\rho_{Ar,I}}}{\left(\frac{D_I}{2}\right)^2 \cdot \pi} = 0.268 \frac{\text{ft}}{\text{s}}$$

Liquid Reynolds number

$$Re_I := \frac{V_I \cdot D_I \cdot \rho_{Ar,I}}{\mu_{Ar,I}} = 7497$$

define initial guesses for calc

$$\text{Guess } f := 0.5$$

Friction factor calculation

$$\text{Given } \frac{1}{\sqrt{f}} = -4.0 \cdot \log \left(\frac{\varepsilon}{3.7 \cdot D_V} + \frac{1.256}{Re_I \cdot \sqrt{f}} \right)$$

Colebrook formula
valid for $Re > 4000$

$$f := \text{Find}(f) \quad f = 0.0086$$

Liquid Pressure drop

$$\Delta P_{liq} := \frac{2 \cdot L_I \cdot \rho_{Ar,I} \cdot \left[\frac{\frac{m\text{flow}_{Ar}}{\rho_{Ar,I}}}{\left(\frac{D_I}{2}\right)^2 \cdot \pi} \right]^2 \cdot f}{D_I} \quad \Delta P_{liq} = 0.052 \text{ psi}$$